

Subject 24

Please, don't write on the exam paper.

Question 1

Let $C_n = 1^3 + 2^3 + \dots + n^3$ ($n \geq 1$)

Prove by recurrence that for any natural number $n \geq 1$:

$$C_n = \frac{n^2(n+1)^2}{4}$$

Question 2

Prove the following statement by contradiction or contrapositive :

If $a^2 - 2a + 7$ is even, then a is **odd**. (a integer)

Nota : **odd** : impair